Does the Balassa-Samuelson hypothesis hold for Asian countries? An empirical analysis using panel data cointegration tests

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Abstract

This paper tests empirically the Balassa-Samuelson (BS) hypothesis using annual data for 6 Asian countries. We apply new panel data cointegration techniques recently developed by Pedroni (2000) and we compare the results with those obtained with conventional Johansen (1995)’s time series cointegration tests.

Whereas, standard time series approach turns out to be able to put in evidence a significant long-run relationship between real exchange rate and productivity differential; this relationship is strongly rejected for all countries using recent advances in the econometrics of non-stationary dynamic panel methods. Closer examinations of the three key components of the BS hypothesis enable us to identify clearly the causes of this empirical failure. We find that the absence of a positive long-run relationship between productivity differential and relative prices is the reason for this rejection.

Keywords: Real Exchange Rate, Balassa-Samuelson hypothesis, Asian countries, Panel unit-root and cointegration tests.

JEL Classification: E31, F0, F31, C15.

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1 Introduction

As it is now well-established economists often refer to two alternative theories to explain long-run real exchange rate movements.

The former is Purchasing Power Parity (PPP) according to which real exchange rate must be stationary. This implies there cannot exist persistent deviations from real exchange equilibrium level, but only temporary ones. In this case PPP serves as a good first approximation to long-run behaviour. Recent empirical evidence supporting this proposition under the current float has however been mixed. Parikh and Wakerly (2000) for instance found empirical evidence in favour of this theory, whereas Fleissig and Strauss (2000) rejected it.

The latter, the Balassa-Samuelson (BS) hypothesis, which seeks to explain the persistence of real exchange rate changes, typically focus on the tradebility of goods. According to Balassa (1964) and Samuelson (1964), rapid economic growth is accompanied by real exchange rate appreciation because of differential productivity growth between tradable (T) and non-tradable (NT) sectors. Since the differences in productivity increases are expected to be larger in high growth countries, the BS prediction should be more visible among fast growing countries. In this respect, the postwar Japanese record is generally recognized to have been a prime example of the BS hypothesis.
Much attention has been paid in literature to test the validity of this hypothesis using time series econometric techniques. Early cointegration tests such as Engle and Granger (1987) cointegrating regression and Johansen (1988), (1995)) maximum likelihood (ML) procedures produce mixed results. Rogoff (1992), DeLoach (2001), Bahmani -Oskooee (1992), Bahmani-Oskooee and Rhee (1996) for instance have all investigated whether real exchange rate changes can be explained by relative productivities, but only the latter two managed to put in evidence such a relationship. Using a slightly different approach Asea and Mendoza (1994), De Gregorio and al (1994) find, using annual, sectorial data from OECD countries, that relative prices are explained by relative productivities, but it is unclear whether real exchange rate can be explained by relative productivities. These diverging conclusions may be attributable to the low power of the tests implemented with short spans of data as argued by many researchers, given the fact that we only have less than 25 years of data for the current float.

A possible way of improving the power of these tests is by introducing cross-section variation. This may explain why methods for non-stationary time series panel, including unit root tests (Levin and Lin (1993), Quah (1994), Im, Pesaran and Shin (1997)), and cointegration tests (Pedroni ((1996), (1997), (1999), (2000)) or Blinder, Hsiao and Pesaran (1999)) have been gaining increased acceptance in empirical research. Recent applica-
tions of these panel tests for cointegration include Taylor (1996) to historical episodes of purchasing power parity, Canzoneri and al (1999) (for OECD countries), Drine and Rault (2003a) (for Latin American countries), and Drine et al. (2003b) (For Central and Eastern Europe) to productivity and real exchange rate.

The contribution of this paper is twofold. Firstly, we investigate empirically the “original” BS hypothesis for six Asian countries which doesn’t reduce itself to the existence of a positive relationship between the relative prices of NT goods and relative labour productivities as it is sometimes assumed in literature. Indeed, in a very schematic way, the Balassa-Samuelson hypothesis can be decomposed into three main assumptions:

(A1) the differential of productivities between T and NT sector and relative prices are positively correlated,

(A2) real exchange rate and the relative prices of NT goods are positively correlated,

(A3) purchasing power parity is verified for tradable goods.

A combination of these assumptions causes real exchange rate appreciation. The interest of proceeding similarly is that in case of refuting empirically the BS hypothesis we can identify precisely which of the above assumption (s) is (are) responsible for this rejection.

Secondly, in contrast to previous works that implemented the standard
time series cointegration tests, we employ the most recent development of cointegration techniques in heterogeneous panels developed by Pedroni (2000) and particularly small sample corrections for fully modified parameter estimates, as well as restriction testing on the parameters of cointegrating relationships.

We consider here annual data for 6 Asian economies (India, Indonesia, Korea, the Philippines, Singapore and Thailand) covering the 1983-1997 period, and we compare the panel data econometric results with those that are obtained with conventional unit-root tests and cointegrating techniques. The econometric investigation shows that standard time series cointegration methods support the BS hypothesis, since they turn out to be able to put in evidence a significant long-run relationship between productivity differential and real exchange rate for 5 countries out of 6. On the contrary, the recent panel cointegration techniques of Pedroni (2000) indicate strong evidence against such a relationship for the six Asian countries. This leads us to examine more precisely the reasons for this failure and to analyze carefully the three key assumptions on which the BS hypothesis rests. This additional step permits us to identify clearly the reason for the BS empirical rejection. Indeed, for all countries we find that this rejection is attributable to the failure of the existence of a significant positive relationship between productivity differential and relative prices (assumption $A_1$).
The remainder of the paper is organised as follows. In Section 2 we briefly review the Balassa-Samuelson framework. Much attention is paid to make explicit where the three key assumptions of this theory intervene. This enables us to derive formally afterwards the different relationships to be tested in the empirical application. In section 3 we present the panel data unit root tests and panel cointegration methodology that will be used in the empirical application. In section 4 we expose and comment our econometric results for 6 Asian countries. A final section reviews the main findings.

2 The Balassa-Samuelson hypothesis revisited

Let us consider a small open economy composed of a set of homogeneous firms. The representative firm produces two goods: a tradable commodity for the world market and a non-tradable one for domestic demand. It is supposed besides that tradable and non-tradable goods production requires both capital and labour. The competition is supposed to be perfect and it ensures that production factors are paid at their marginal productivity; labour factor mobility ensures equal pay. Labour supply is supposed to be constant and all variables are expressed in terms of tradable goods.

As noted by Obstfeld and Rogoff (1996), in the absence of nominal rigidity, equilibrium real exchange rate will only depend on productivity differential. Thus in what follows we present a partial equilibrium model where
the demand side is absent.

2.1 Firm behaviour

The representative firm maximises its intertemporal profit expressed in terms of tradable goods under its constraints of technology and capital accumulation, that is:

\[
\max \int_0^\infty \left( y_e(k_e, l_e) + p y_n(k_n, l_n) - wt - i \right) e^{-rt} dt
\]

(1)

\[sck = i - \delta k\]

(2)

where,

- \(y_e\) denotes the production of tradable goods;
- \(y_n\) denotes the production of non-tradable goods;
- \(p\) denotes the relative prices of non-tradable goods in terms of tradable ones;
- \(i\) denotes investment;
- \(w\) denotes wages;
- \(k\) denotes capital;
- \(r\) denotes foreign interest rate;
• $l = l_n + l_e$ is labour supply.

2.2 Equilibrium

The equilibrium is defined as follows

$$\frac{\delta y_e}{\delta k_e} = p \frac{\delta y_n}{\delta k_n} = r$$  \hspace{1cm} (3)

$$\frac{p \delta y_n}{\delta l_n} = \frac{\delta y_e}{\delta l_e} = w$$  \hspace{1cm} (4)

$$\lambda = 1$$  \hspace{1cm} (5)

We thus obtained the following relationship between relative prices and labour productivity ratio :

$$\frac{\delta y_e}{\delta l_e} = p \frac{\delta y_n}{\delta l_n}$$  \hspace{1cm} (6)

For Cobb-Douglas functions, this relation expresses as :

$$p = \frac{\alpha \theta_e}{\beta \theta_n}$$  \hspace{1cm} (7)

where $\alpha$ and $\beta$ are the production-labour elasticities respectively for tradable and non-tradable sectors and $\theta_n$, $\theta_e$ the labour average productions for the two sectors.
Equation (7) indicates that relative prices are a function of the productivity ratio of the two goods. Thus a faster increase of tradable goods productivity than of non-tradable ones leads to an increase in relative prices of non-tradables (Assumption A1).

Furthermore real exchange rate is defined as:

$$e = \frac{P}{EP^*}$$

(8)

where,

E denotes nominal exchange rate,

P denotes general domestic price index,

$P^*$ denotes general foreign price index.

If we suppose that the consumer’s basket contains two commodities, we can express the general price index as:

$$P = P_eP_n^{1-\epsilon} \text{ and } P^* = (P^*_e)^\epsilon(P^*_n)^{1-\epsilon}$$

(9)

Then, following Balassa and Samuelson and if we suppose that purchasing power parity in the tradable sector (Assumption 2) is verified, we will have:

$$\log(e) = (1 - \epsilon) \log(p) - (1 - \epsilon)\log(p^*)$$

(10)

1 Real exchange rate is defined in the following way: an increase implies an appreciation.
where,

\( p \) denotes relative domestic price for nontradable goods,

\( p^* \) denotes relative foreign price for nontradable goods.

According to equation (10) real exchange rate is positively correlated to the relative prices of non-traded goods (Assumption A3).

Taking the above analysis into account (A1, A2, and A3), we obtain the “general” BS relationship:

\[
\log(e) = \phi + (1 - \epsilon)[\log(\theta_e) - \log(\theta_e^*)] \quad (11)
\]

This relationship indicates that relative productivity differential determines the long-term real exchange rate behaviour.

3 Econometric methodology

We now present the panel unit root tests and panel cointegration tests that we will use in the empirical application reported in section 4.

3.1 Panel unit root tests

Initial methodological work on non-stationary panels focused on testing unit roots in univariate panels. Quah (1994) derived standard normal asymptotic distributions for testing unit roots in homogeneous panels as both time series and cross sectional dimension grow large. Levin and Lin (1993)
derived distributions under more general conditions that allow for heterogeneous fixed effects and time trend. More recently, Im, Pesaran and Shin (1997), studied the small properties of unit root tests in panels with heterogeneous dynamics and proposed alternative tests based on the mean of individual unit-root statistics. In this paper we shall apply Im, Pesaran and Shin (1997) unit-root test (called IPS after) since it is more powerful than those of Quah (1994) and Levin and Lin (1993) used in existing studies.

Levin and Lin’s test is considered as more general than those of Quah since it explicitly takes heterogeneity and correlation between units into account. However as shown by Papell (1997) it suffers from size distortion without being able to correct serial correlation adequately. Using Monte Carlo simulations, he showed that the finite sample critical values are greater than those in Levin and Lin (1993). For quarterly data, the critical values are 11% higher (on average) than those reported by Levin and Lin and for monthly data, they are 3% higher.

The test proposed by Im, Pesaran and Shin (1997) permits to solve Levin and Lin’s serial correlation problem in assuming heterogeneity between units in a dynamic panel framework. Furthermore as shown by Im and al via Monte Carlo simulations it has higher power than that of Levin and Lin. IPS (1997) propose two statistics : a Maximum Likelihood Statistics, called Lbar, and a Student statistic tb. These two statistics are based on individual
Augmented Dickey-Fuller (ADF) regressions. Since an appropriate ADF regression will correct the serial correlation in the data, the IPF panel unit-root test takes care of serial correlation automatically. In our empirical work of section 4 we shall use the $t_b$ statistic instead of the $L_{bar}$ one since IPS’s Monte Carlo experiments have shown that it is the more powerful even for a value of $N$ inferior to 5. This statistic can be expressed as:

$$t_b = \frac{\sqrt{N}(t_{NT} - E(t_T))}{\sqrt{Var(t_T)}}$$

where $t_{NT} = \frac{1}{N} \sum_{i=1}^{N} t_{iT}$ is an average of the $t$ individual student statistic in a conventional time series unit-root analysis, $E(t_T)$ and $V(t_T)$ are respectively the mean and variance of $t_{iT}$ under the null hypothesis that the series are integrated of order one with $N \to \infty$.

IPS show that under the null hypothesis of non-stationarity, the $t_b$ statistic follows the standard normal distribution asymptotically.

### 3.2 Panel cointegration tests

In the empirical application we shall apply Pedroni’s cointegration test methodology (1995a, 1997 and 1999) to analyse the Balassa-Samuelson hypothesis. Pedroni (1995a) studied the properties of spurious regressions and tests for cointegration in heterogeneous panels and derived appropriate distributions for these cases. These allow one to test for the presence of long
run equilibria in multivariate panels while permitting the dynamic and even the long run cointegrating vectors to be heterogeneous across individual members. Like the IPS panel unit-root test, the panel cointegration tests proposed by Pedroni also take heterogeneity into account using specific parameters which of course are allowed to vary across individual members of the sample. Pedroni (1997 and 1999) derived the asymptotic distributions and explored the small sample performances of seven different statistics to test panel data cointegration. Of these seven statistics, four are based on pooling along, what is often referred to as the Within dimension (called “panel” after), and the last three ones are based on the Between dimension (called “group” after). These different statistics are based on a model that assumes that cointegration relationships are heterogeneous between individual members and are defined as:

For the Within statistics

\[
Z_w^\rho = \left( \sum_{i=1}^{N} \sum_{t=1}^{T} L_{11i}\hat{e}_{it}^2 \right)^{-1} \sum_{i=1}^{N} \sum_{t=1}^{T} L_{11i}(\hat{e}_{it-1}\Delta \hat{e}_{it} - \hat{\lambda}_i) : \text{Panel Rho}_\text{stat}
\]

\[
Z_w^{\text{ADF}} = (\sum_{i=1}^{N} \sum_{t=1}^{T} L_{11i}\hat{e}_{it}^{*2})^{-1/2} \sum_{i=1}^{N} \sum_{t=1}^{T} L_{11i}(\hat{e}_{it-1}\Delta \hat{e}_{it}^*) : \text{Panel Adf}_\text{stat}
\]

\[
Z_w^{PP} = (\sum_{i=1}^{N} \sum_{t=1}^{T} L_{11i}\hat{e}_{it-1}^2)^{-1/2} \sum_{i=1}^{N} \sum_{t=1}^{T} L_{11i}(\hat{e}_{it-1}\Delta \hat{e}_{it} - \hat{\lambda}_i) : \text{Panel PP}_\text{stat}
\]

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\[ Z_v^w = \left( \sum_{i=1}^{N} \sum_{t=1}^{T} \Delta \sum_{t=1}^{T} (\tilde{\epsilon}_{it-1} \Delta \tilde{\epsilon}_{it} - \tilde{\lambda}_i) \right)^{-1} : \text{Panel V\_stat} \]

For the Between statistics

\[ Z_{\rho}^{B} = \sum_{i=1}^{N} \left( \sum_{t=1}^{T} \hat{\epsilon}_{i,t-1}^2 \right)^{-1} \sum_{t=1}^{T} (\hat{\epsilon}_{it-1} \Delta \hat{\epsilon}_{it} - \hat{\lambda}_i) : \text{Group Rho\_stat} \]

\[ Z_{t}^{B} = \sum_{i=1}^{N} \left( \sum_{t=1}^{T} \hat{\epsilon}_{i,t-1}^2 \right)^{-1} \sum_{t=1}^{T} (\hat{\epsilon}_{it-1} \Delta \hat{\epsilon}_{it} - \hat{\lambda}_i) : \text{Group Adf\_stat} \]

\[ Z_{pp}^{B} = \sum_{i=1}^{N} \left( \sum_{t=1}^{T} \hat{s}_{i,t-1}^{2} \hat{\epsilon}_{i,t}^{2} \right)^{-1} \sum_{t=1}^{T} (\hat{\epsilon}_{it-1} \Delta \hat{\epsilon}_{it}^{*} ) : \text{Group PP\_stat} \]

with,

\[ \hat{\lambda} = \frac{1}{T} \sum_{s=1}^{k_i} (1 - \frac{s}{k_i+1}) \sum_{t=s+1}^{T} \mu_{it} \mu_{it-s}, \]

\[ \hat{s}_{i}^{2} = \frac{1}{T} \sum_{t=s+1}^{T} \hat{\mu}_{it}^{2}, \hat{\sigma}^{2} = s_{i}^{2} + 2\hat{\lambda}_{i}, \]

\[ \tilde{\sigma}_{i}^{2} = \hat{s}_{i}^{2} + 2\hat{\lambda}_{i}, \]

\[ \tilde{\sigma}_{NT}^{2} \frac{1}{T} \sum_{i=1}^{N} \hat{L}_{i}^{-2} \hat{\sigma}_{i}^{2}, \]

\[ \hat{s}^{*2} = \frac{1}{T} \sum_{t=s+1}^{T} \hat{\mu}_{it}^{2}, \tilde{s}^{*2}_{NT} = \frac{1}{T} \sum_{t=s+1}^{T} \hat{s}^{*2}_{i}, \hat{L}_{11i}^{2} \sum_{t=1}^{T} \tilde{\eta}_{it}^{2} + \frac{1}{T} \sum_{s=1}^{k_i} (1 - \frac{s}{k_i+1}) \sum_{t=1}^{T} \tilde{\eta}_{it} \tilde{\eta}_{it-s} \]

and where the residuals are extracted from the above regressions:

\[ \hat{\epsilon}_{it} = \hat{\rho} \hat{\epsilon}_{it-1} + \hat{u}_{it}, \]
\[ \hat{e}_{it} = \hat{\rho} \hat{e}_{it-1} + \sum_{k=1}^{K} \hat{\gamma}_{ik} \Delta \hat{e}_{it-k} + \hat{\mu}_{it}, \]
\[ \Delta y_{it} = \sum_{m=1}^{M} \hat{b}_{mi} \Delta X_{mit} + \hat{\eta}_{it}, \]

Note that in the above writings \( L_i \) represents the \( i^{th} \) component of the Cholesky decomposition of the residual Variance-Covariance matrix, \( \hat{\lambda} \) and \( \hat{\sigma}_{NT} \) are two parameters used to adjust the autocorrelation in the model, \( \sigma_i \) and \( \sigma_i^2 \) are the contemporaneous and long-run individual variances.

Pedroni has shown that the asymptotic distribution of these seven statistics can be expressed as:

\[ \frac{\chi_{NT} - \mu \sqrt{N}}{\sqrt{\nu}} \rightarrow N(0, 1) \]

where \( \chi_{NT} \) is the statistic under consideration among the seven proposed, \( N \) and \( T \) are the sample parameter values and \( \mu \) and \( \nu \) are parameters tabulated in Pedroni (1999).

In terms of power Pedroni (1997) showed that for values of \( T \) larger than 100, all the proposed seven statistics do fairly well and are quite stable. However for smaller samples (\( T \) inferior to 20) the Group ADF-Statistic (non-parametric) is the most powerful, followed by the Panel v-Statistic and the Panel rho-Statistic. For this reason, \textit{only the group ADF-statistic will be considered in our study for panel cointegration testing}. The finite sample distribution for the seven statistics have been tabulated by Pedroni.
(1997) via Monte Carlo simulations. The calculated test statistics must be larger (in absolute value) than the tabulated critical value to reject the null hypothesis of absence of cointegration.

4 Empirical investigation

4.1 The data

We include 6 Asian countries in our sample (India, Indonesia, Korea, the Philippines, Singapore and Thailand). The choice of countries is based on data availability. The empirical period starts in 1983 and ends in 1998, corresponding to 15 observations for the time series dimension. The effective real exchange rate (RER) data are taken from the French database of the CEPII. RER is defined as the ratio between the domestic price index and the foreign price one with respect to the USA multiplied by the nominal exchange rate (so a RER increase indicates an appreciation). The added sectorial value and employment series are taken from the “World Table” of “the Asian Bank’s Key Indicators of Developing Asian and Pacific Countries”. The traded sector is composed of the “manufacturing” sector and the “agriculture, hunting, forestry and fishing” sector. The non-traded sector is composed of the service sector (transport, storage and communication, finance, insurance, real estate and business services). The traded price index is the added value deflator of each sector. Average productivities for
tradable and non-tradable sectors are defined as the added value divided by employment.

4.2 Unit-Root test results

We shall report in this sub-section the results of two kinds of unit-root tests: the conventional time series ones and the Im, Pesaran and Shin (IPS, 1997) panel data ones.

The analysis first step is simply to look at the data univariate properties and to determine their integratedness degree. Theoretically a process is either I(0), I(1) or I(2). Nevertheless in practice many variables or variable combinations are borderline cases, so that distinguishing between a strongly autoregressive I(0) or I(1) process (interest rates are a typical example), between a strongly autoregressive I(1) or I(2) process (nominal prices are a typical example) is far from being easy. We have therefore applied a sequence of standard time series unit root tests (Schmidt and Phillips test (1992), Kwiatkowsky, Phillips and Shin test (KPSS) (1992) and the efficient unit-root tests suggested by Elliott, Rothenberg and Stock (1996) (which we shall refer to hereafter as the ERS test)), to investigate which of the I(0), I(1), I(2) assumption is most likely to hold. The results of these conventional unit-root tests are not reported here to save space but they can easily be summarised as follows since clear patterns emerge from them\(^2\). Indeed, they

\(^2\)The results of these tests are available upon request.
indicate that the unit-root null hypothesis cannot be rejected at the 5% level for the three variables under consideration (RER, productivity differential between tradable and non-tradable sectors, relative prices) and for all our Asian countries. We have also applied those three tests on the variables taken in first differences and we find evidence in favour of the rejection of the non-stationary hypothesis for our three series. This leads us to conclude that our series are well characterised as an I(1) process, some with non-zero drift for some countries.

As far as the IPS (1997) panel data unit-root test is concerned (which we have applied for a model with a constant, and for both a constant and a trend), it indicates that for all 6 Asian countries the unit-root hypothesis cannot be rejected for all series (see table 1 in Appendix).

4.3 Cointegration test results

The following panel data formalisation of the Balassa-Samuelson’s framework presented in section 2 is fairly straightforward to derive. Indeed, using previous notations the long-run relationship (corresponding to the BS hypothesis) to be tested can be written as:

\[
\log(RER_{it}) = c_i + \gamma_i \log(\frac{\theta_{nit}}{\theta_{nit}^*}) + \epsilon_{it} \tag{12}
\]

According to BS predictions, we expect \(\gamma_i\) to be positive since an increase of real exchange rate implies an appreciation.
In the same way, if empirical evidence doesn’t support the BS hypothesis, the three key assumptions ($A_1$, $A_2$, $A_3$) to be tested in order to identify the reason(s) for this rejection write as follows:

\begin{align*}
A_1 & : \log(p_{it}) = c_{1i} + \gamma_{1i} \log(\theta_{eit}/\theta_{nit}) + \varepsilon_{1it} \\
A_2 & : \log(RER_{it}) = c_{2i} + \gamma_{2i} \log(p_{it}) + \varepsilon_{2it} \\
A_3 & : P_T = E P_T^* \end{align*}

The results of the cointegration analysis are reported in Appendix. We consider both time series cointegration tests (see table 2) as well as panel cointegration tests developed by Pedroni (2000) (see table 3), with sample size corrections for small samples like ours. Table 2 reports the results of Johansen’s (1988, 1995) conventional time series cointegration tests. It appears that for 5 countries out of 6 (India, Indonesia, the Philippines, Singapore and Thailand) the hypothesis of the absence of cointegration between real exchange rate and productivity differential can be rejected at a 5% level of significance. Thus the findings of cointegration time series tests are consistent with the BS hypothesis.
The implementation of Pedroni’s recent panel data cointegration tests (2000) leads to an opposed result since the theoretical long-run relationship between real exchange rate and productivity differential is now strongly rejected at a 5% level of significance (see Table 3). This result shows the superiority of panel data cointegration tests which are more powerful than conventional time series ones and underlines the necessity to be cautious when interpreting usual time series test results for samples of relatively moderate size. These results suggest that productivity differential doesn’t correctly account for long-run real exchange rate movements for our 6 Asian economies. In order to shed some light on the origin of that rejection of the BS hypothesis, our next task is to examine successively each three key component of this hypothesis.

The first key component of the BS hypothesis (A1) postulates that productivity differential between tradable and non-tradable sectors and relative prices are positively correlated. Empirical evidence from Pedroni’s panel cointegration test (2000) reported in Table 3 rejects strongly this assumption at a 5% level of significance since we were not able to confirm the existence of a significant long-run relationship between these two variables (see Table 3).

Then, we investigate the second key component of the BS hypothesis, that is that real exchange rate and relative prices of non-traded goods are
positively correlated. Here we are able to put in evidence a long-run sta-
tistical relationship between these two variables for all Asian countries (see Table 3).

Finally, we test the third key component of the BS hypothesis (A3) i.e. that PPP holds for tradable goods (which implies that the nominal ex-
change rates and PPP exchange rates are cointegrated with a cointegrating slope of 1.0). We investigate using a t-test if the slope in the cointegrating relationship is equal to 1, as predicted by Balassa-Samuelson. To get robust results and avoid well-known small sample problems, we estimate our long-run parameters using small sample corrections recently proposed by Pedroni (2000). The empirical results (reported in Table 4) do support this unitary theoretical relationship which is accepted by data at a 5 % level of significance, the fully modified OLS slope estimates being only of 0.74 with a T-Ratio of 1.66 for the null hypothesis that $\beta_{1i} = 1.0$. This finding is in accordance with the acceptance of the second component tested previously.

Thus, the main conclusion which emerges from the above analysis is that the failure of the BS hypothesis for the countries can be attributed to the rejection of the first key component of this hypothesis. Indeed, empirical evidence clearly indicates that productivity differential between tradable and non-tradable sectors and relative prices are not cointegrated.
5 Conclusion

So, do Pedroni’s recent cointegration techniques (2000) which enable to deal with non-stationary data in heterogeneous panels, as well as with small sample size, permit to rescue the Balassa-Samuelson hypothesis?

The evidence from a panel of 6 Asian countries reveals that these new methods do much better than usual time series cointegration ones (see Johansen (1988), (1995)), since unlike the latter, they indicate the absence of a significant cointegrating relationship between real exchange rate and productivity differential.

One possible reason is that the main assumptions that comprise the BS hypothesis are not verified. Thus, questioning for the reasons of this failure led us to examine separately the validity of each of the three key components of the BS hypothesis. This empirical analysis is rich of teachings and allows us to clearly identify why this theory is not confirmed for all Asian economies. We find that the rejection of the BS hypothesis can be accounted for by the rejection of the expected positive long-run relationship between relative prices of non-traded goods and productivity differential. A possible explanation of the BS empirical rejection may simply be that there are additional long-run real exchange determinants that have to be considered.
Aknowledgements

We would like to thank Peter Pedroni for providing us with some RATS
codes for the computation of the critical values, making the panel cointe-
gration tests available in this present analysis, as well as for his modified
group-fm program for small sample adjustments.
References


### Appendix: Unit-root and cointegration test results for 6 Asian Countries

#### Table I. Panel Unit Root tests (ADF test statistics)  
* (Im, Pesaran and Shin (1997))

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<th>Real exchange rate</th>
<th>Ln (TCR)</th>
<th>Level</th>
<th>First difference</th>
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<td>Constant and trend</td>
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<table>
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<th>Ln (Pmn)</th>
<th>Level</th>
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<td>Constant and trend</td>
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<td></td>
<td>1.27</td>
<td>1.43</td>
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</table>

#### Table II. Conventional cointegration tests (Johansen (1995))

**Test of the Balassa-Samuleson hypothesis** i.e the existence of a long-run relationship between Real exchange rate and Productivity differential

<table>
<thead>
<tr>
<th>Country</th>
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<th>L_max 1</th>
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<th>Trace 1</th>
<th>Number of cointegrating relationships</th>
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</thead>
<tbody>
<tr>
<td>India</td>
<td>14.571</td>
<td>3.321</td>
<td>17.89</td>
<td>3.321</td>
<td>1</td>
</tr>
<tr>
<td>Indonesia</td>
<td>14.341</td>
<td>3.711</td>
<td>17.051</td>
<td>3.711</td>
<td>1</td>
</tr>
<tr>
<td>Korea,</td>
<td>6.106</td>
<td>0.570</td>
<td>6.677</td>
<td>0.570</td>
<td>0</td>
</tr>
<tr>
<td>The Philippines</td>
<td>16.581</td>
<td>3.257</td>
<td>16.841</td>
<td>3.257</td>
<td>1</td>
</tr>
<tr>
<td>Singapore</td>
<td>15.322</td>
<td>3.719</td>
<td>15.541</td>
<td>3.719</td>
<td>1</td>
</tr>
<tr>
<td>Thailand</td>
<td>17.106</td>
<td>3.570</td>
<td>6.677</td>
<td>3.570</td>
<td>1</td>
</tr>
</tbody>
</table>

---

1 The critical value at a 5% level is –1.65.
2 The critical value at a 5% level is –1.65.
3 The critical value at a 10% level is 14.1.
4 The critical value at a 10% level is 3.8.
5 The critical value at a 10% level is 15.4.
6 The critical value at a 10% level is 3.8.
Table III: Panel Cointegration tests (Pedroni (1996, 2000))

<table>
<thead>
<tr>
<th>Test statistics</th>
<th>6 countries, 2 variables ln (TCR), ln (Pmn)</th>
<th>6 countries, 2 variables ln (Ptn), ln (Pmn)</th>
<th>6 countries, 2 variables ln (TCR), ln (Ptn)</th>
</tr>
</thead>
<tbody>
<tr>
<td>panel v-stat</td>
<td>1.22294</td>
<td>0.55707</td>
<td>-0.77056</td>
</tr>
<tr>
<td>panel rho-stat</td>
<td>-0.3084</td>
<td>-0.35934</td>
<td>1.26434</td>
</tr>
<tr>
<td>panel pp-stat</td>
<td>-0.92083</td>
<td>-1.35555</td>
<td>1.38549</td>
</tr>
<tr>
<td>panel adf-stat</td>
<td>-1.05016</td>
<td>-1.2938</td>
<td>1.78278</td>
</tr>
<tr>
<td>group rho-stat</td>
<td>0.16321</td>
<td>0.76197</td>
<td>1.84372</td>
</tr>
<tr>
<td>group pp-stat</td>
<td>-0.90071</td>
<td>-0.78468</td>
<td>1.60162</td>
</tr>
<tr>
<td>group adf-stat</td>
<td>-0.6258</td>
<td>-0.64517</td>
<td>1.78788</td>
</tr>
</tbody>
</table>

Note: In the Pedroni-Rats code a value of 2 is chosen for the m lag option, but the conclusions concerning the acceptance/rejection of the null hypothesis of no cointegration are not sensitive to the value of the lag truncation (m lag = 1, 2, 3).

Table IV. Panel test for PPP in tradable sector for 6 Asian countries Pedroni (2000)

<table>
<thead>
<tr>
<th>Country</th>
<th>Cointegrating coefficient</th>
<th>t-stat</th>
</tr>
</thead>
<tbody>
<tr>
<td>India</td>
<td>0.69</td>
<td>-1.38</td>
</tr>
<tr>
<td>Indonesia</td>
<td>0.98</td>
<td>-0.15</td>
</tr>
<tr>
<td>Korea</td>
<td>1.68</td>
<td>-1.59</td>
</tr>
<tr>
<td>The Philippines</td>
<td>0.86</td>
<td>-2.35</td>
</tr>
<tr>
<td>Singapore</td>
<td>0.99</td>
<td>-1.60</td>
</tr>
<tr>
<td>Thailand</td>
<td>0.62</td>
<td>-1.38</td>
</tr>
<tr>
<td>Average Coefficient</td>
<td>0.74</td>
<td>1.66⁷</td>
</tr>
</tbody>
</table>

It is important here to stress that the rejection of the panel null hypothesis of no cointegration for a set of countries means that there exist a cointegrating relationship for each country of the panel (cf. Pedroni). Let us give a simple example to illustrate this.

Imagine that each member of the panel represents a draw from an underlying population. The panel in this case simply represents a repeated sampling, N times, from an underlying population. In this case, the population DGP either is cointegrated or is not cointegrated. As you increase the number of individuals of the panel, you are simply accumulating information regarding whether or not the population DGP is cointegrated or is not cointegrated. In this case, the proper interpretation of the panel test is:

Null hypothesis: The DGP is not cointegrated, Alternative hypothesis: The DGP is cointegrated

This translates, for the panel, into the statement: Null hypothesis: No individuals are cointegrated, Alternative hypothesis: All individuals are cointegrated. Under this interpretation, there is no such thing as one individual being cointegrated and the others not being cointegrated. The appearance of possible contradictions based on individual tests is simply a consequence of sampling error in the estimator, not differences in the truth regarding cointegration.

This interpretation is useful in practice when you have a theory that says, if the theory is correct as a general description of the way the world works, then two variables should be cointegrated, regardless of which country the variables come from.

Pedroni (1996 and 2000) derived the asymptotic distributions and explored the small sample performances of seven different statistics to test cointegration on panel data. Of these seven statistics, four are based on pooling along, what is often referred to as the Within dimension and the last three ones are based on the Between dimension. These different statistics are based on a model that assumes that cointegration relationships are heterogeneous between individual members (See Pedroni for further details).

The critical value at a 5% level is –1.65. The calculated test statistics must be larger (in absolute) value than the tabulated critical value to reject the null hypothesis of absence of cointegration.

⁷ T-stats are for the null hypothesis that the estimated coefficient is equal to 1.